

- 3: **n** – Integer *Input*
On entry: n , the order of the matrix B .
Constraint: $n \geq 0$.
- 4: **kb** – Integer *Input*
On entry: k , the number of super-diagonals of the matrix B if **uplo** = **Nag_Upper**, or the number of sub-diagonals if **uplo** = **Nag_Lower**.
Constraint: $kb \geq 0$.
- 5: **bb**[*dim*] – Complex *Input/Output*
Note: the dimension, *dim*, of the array **bb** must be at least $\max(1, \mathbf{pddb} \times \mathbf{n})$.
On entry: the n by n Hermitian band matrix B . This is stored as a notional two-dimensional array with row elements or column elements stored contiguously. The storage of elements b_{ij} depends on the **order** and **uplo** parameters as follows:
 if **order** = **Nag_ColMajor** and **uplo** = **Nag_Upper**,
 b_{ij} is stored in **bb**[$k + i - j + (j - 1) \times \mathbf{pddb}$], for $i = 1, \dots, n$ and
 $j = i, \dots, \min(n, i + k)$;
 if **order** = **Nag_ColMajor** and **uplo** = **Nag_Lower**,
 b_{ij} is stored in **bb**[$i - j + (j - 1) \times \mathbf{pddb}$], for $i = 1, \dots, n$ and
 $j = \max(1, i - k), \dots, i$;
 if **order** = **Nag_RowMajor** and **uplo** = **Nag_Upper**,
 b_{ij} is stored in **bb**[$j - i + (i - 1) \times \mathbf{pddb}$], for $i = 1, \dots, n$ and
 $j = i, \dots, \min(n, i + k)$;
 if **order** = **Nag_RowMajor** and **uplo** = **Nag_Lower**,
 b_{ij} is stored in **bb**[$k + j - i + (i - 1) \times \mathbf{pddb}$], for $i = 1, \dots, n$ and
 $j = \max(1, i - k), \dots, i$.
On exit: B is overwritten by the elements of its split Cholesky factor S .
- 6: **pddb** – Integer *Input*
On entry: the stride separating row or column elements (depending on the value of **order**) of the matrix B in the array **bb**.
Constraint: $\mathbf{pddb} \geq \mathbf{kb} + 1$.
- 7: **fail** – NagError * *Output*
 The NAG error parameter (see the Essential Introduction).

6 Error Indicators and Warnings

NE_INT

On entry, **n** = $\langle value \rangle$.

Constraint: $\mathbf{n} \geq 0$.

On entry, **kb** = $\langle value \rangle$.

Constraint: $\mathbf{kb} \geq 0$.

On entry, **pddb** = $\langle value \rangle$.

Constraint: $\mathbf{pddb} > 0$.

NE_INT_2

On entry, **pddb** = $\langle value \rangle$, **kb** = $\langle value \rangle$.

Constraint: $\mathbf{pddb} \geq \mathbf{kb} + 1$.

NE_CONVERGENCE

The factorization could not be completed, because updated element $b(\langle value \rangle, \langle value \rangle)$ would be the square root of a negative number. Hence B is not positive definite. This may indicate an error in forming the matrix B .

NE_ALLOC_FAIL

Memory allocation failed.

NE_BAD_PARAM

On entry, parameter $\langle value \rangle$ had an illegal value.

NE_INTERNAL_ERROR

An internal error has occurred in this function. Check the function call and any array sizes. If the call is correct then please consult NAG for assistance.

7 Accuracy

The computed factor S is the exact factor of a perturbed matrix $B + E$, where

$$|E| \leq c(k+1)\varepsilon|S^H||S|,$$

$c(k+1)$ is a modest linear function of $k+1$, and ε is the *machine precision*. It follows that $|e_{ij}| \leq c(k+1)\varepsilon\sqrt{(b_{ii}b_{jj})}$.

8 Further Comments

The total number of floating-point operations is approximately $4n(k+1)^2$, assuming $n \gg k$.

A call to this function may be followed by a call to `nag_zhbgst (f08usc)` to solve the generalized eigenproblem $Az = \lambda Bz$, where A and B are banded and B is positive-definite.

The real analogue of this function is `nag_dpbstf (f08ufc)`.

9 Example

See Section 9 of the document for `nag_zhbgst (f08usc)`.